#### **Computer Graphics**

#### **6** - Viewing, Projection

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# **Topics Covered**

- Rendering Pipeline
  - Vertex Processing
    - Viewing transformation
    - Projection Transformation
    - Viewport Transformation

#### **Vertex Processing (Transformation Pipeline)**



# **Viewing Transformation**



### **Recall that...**

- 1. Placing objects
- $\rightarrow$  Modeling transformation
- 2. Placing the "camera"
  → Viewing transformation
- 3. Selecting a "lens"
- $\rightarrow$  **Projection transformation**
- 4. Displaying on a "cinema screen"
- $\rightarrow$  Viewport transformation

# **Viewing Transformation**



- Placing the camera and expressing all object vertices from the camera's point of view
- Transform from world to view space is traditionally called the *viewing matrix*,  $M_v$

# **Viewing Transformation**

- Placing the camera
- → How to set the camera's position & orientation?

- Expressing all object vertices from the camera's point of view
- → How to define the camera's coordinate system (frame)?

#### 1. Setting Camera's Position & Orientation

- Many ways to do this
- One intuitive way is using:
- Eye point
  - Position of the camera
- Look-at point
  - The target of the camera

#### • Up vector

- Roughly defines which direction is up



#### 2. Defining Camera's Coordinate System

Given eye point, look-at point, up vector, we can get camera frame (P<sub>eve</sub>, u, v, w).

– For details, see 6-reference-viewing.pdf



W

#### Viewing Transformation is the Opposite Direction



$$\mathbf{M}_{\mathbf{v}} = \begin{bmatrix} \mathbf{u}_{\mathbf{x}} & \mathbf{v}_{\mathbf{x}} & \mathbf{W}_{\mathbf{x}} & \mathbf{P}_{eyex} \\ \mathbf{u}_{\mathbf{y}} & \mathbf{v}_{\mathbf{y}} & \mathbf{W}_{\mathbf{y}} & \mathbf{P}_{eyey} \\ \mathbf{u}_{\mathbf{z}} & \mathbf{v}_{\mathbf{z}} & \mathbf{W}_{\mathbf{z}} & \mathbf{P}_{eyez} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{1} \end{bmatrix} = \begin{bmatrix} u_{x} & u_{y} & u_{z} & -\mathbf{u} \cdot \mathbf{p}_{eye} \\ v_{x} & v_{y} & v_{z} & -\mathbf{v} \cdot \mathbf{p}_{eye} \\ w_{x} & w_{y} & w_{z} & -\mathbf{w} \cdot \mathbf{p}_{eye} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

#### gluLookAt()



gluLookAt ( $eye_x, eye_y, eye_z, at_x, at_y, at_z, up_x, up_y, up_z$ ) : creates a viewing matrix and right-multiplies the current transformation matrix by it

 $C \leftarrow CM_v$ 

#### [Practice] gluLookAt()

```
import glfw
from OpenGL.GL import *
from OpenGL.GLU import *
import numpy as np
qCamAnq = 0.
qCamHeight = .1
def render():
    # enable depth test (we'll see details later)
    glClear (GL COLOR BUFFER BIT | GL DEPTH BUFFER BIT)
    glEnable(GL DEPTH TEST)
    qlLoadIdentity()
    # use orthogonal projection (we'll see details later)
    glOrtho(-1,1, -1,1, -1,1)
    # rotate "camera" position (right-multiply the current matrix by viewing
matrix)
    # try to change parameters
    gluLookAt(.1*np.sin(gCamAng),gCamHeight,.1*np.cos(gCamAng), 0,0,0, 0,1,0)
    drawFrame()
    glColor3ub(255, 255, 255)
    drawTriangle()
```

```
def drawFrame():
    glBegin(GL LINES)
    glColor3ub(255, 0, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([1.,0.,0.]))
    qlColor3ub(0, 255, 0)
                                                    def main():
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([0.,1.,0.]))
    glColor3ub(0, 0, 255)
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,1.]))
                                                    None, None)
    glEnd()
def drawTriangle():
    glBegin(GL TRIANGLES)
    glVertex3fv(np.array([.0,.5,0.]))
    glVertex3fv(np.array([.0,.0,0.]))
    glVertex3fv(np.array([.5,.0,0.]))
    glEnd()
def key callback (window, key, scancode, action,
mods):
    global gCamAng, gCamHeight
    if action==glfw.PRESS or action==glfw.REPEAT:
        if key==glfw.KEY 1:
            gCamAng += np.radians(-10)
        elif key==glfw.KEY 3:
            gCamAng += np.radians(10)
        elif key==glfw.KEY 2:
            gCamHeight += .1
        elif key==glfw.KEY W:
            gCamHeight += -.1
```

```
if not glfw.init():
        return
    window =
glfw.create window(640,640,'gluLookAt()',
    if not window:
        glfw.terminate()
        return
    glfw.make context current(window)
    glfw.set key callback(window,
key callback)
```

#### while not

```
glfw.window should close (window):
        glfw.poll events()
        render()
        glfw.swap buffers(window)
```

```
glfw.terminate()
```

```
if name == " main ":
   main()
```

# **Moving Camera vs. Moving World**

- Actually, these are two **equivalent operations**
- Translate camera by (1, 0, 2) = Translate world by (-1, 0, -2)
- Rotate camera by  $60^{\circ}$  about y ==Rotate world by  $-60^{\circ}$  about y



# Moving Camera vs. Moving World

- Thus you also can use glRotate\*() or glTranslate\*() to manipulate the camera!
- Using gluLookAt() is just one option of many other choices to manipulate the camera.
- By default, OpenGL places a camera at the origin pointing in negative z direction.



#### **Modelview Matrix**

• As we've just seen, moving camera & moving world are equivalent operations.

 That's why OpenGL combines a viewing matrix M<sub>v</sub> and a modeling matrix M<sub>m</sub> into a modelview matrix M=M<sub>v</sub>M<sub>m</sub>

# Quiz #1

- Go to <u>https://www.slido.com/</u>
- Join #cg-hyu
- Click "Polls"
- Submit your answer in the following format:
  - Student ID: Your answer
  - e.g. 2017123456: 4)
- Note that you must submit all quiz answers in the above format to be checked for "attendance".

### **Projection Transformation**



### **Recall that...**

- 1. Placing objects
- $\rightarrow$  Modeling transformation
- 2. Placing the "camera"
- $\rightarrow$  Viewing transformation (covered in the last class)
- 3. Selecting a "lens"
- $\rightarrow$  Projection transformation
- 4. Displaying on a "cinema screen"
- $\rightarrow$  Viewport transformation

#### **Review:Normalized Device Coordinates**

- Remember that you could draw the triangle anywhere in a 2D square ranging from [-1, -1] to [1, 1].
- Called normalized device coordinates (NDC)

Also known as canonical view volume



#### **Canonical View "Volume"**

- Actually, a canonical view volume is a **3D cube** ranging from [-1,-1,-1] to [1,1,1] in OpenGL
  - Its coordinate system is NDC
- Its **xy** plane is a 2D "viewport"
- Note that NDC in OpenGL is a left-handed coordinate system
  - Viewing direction in NDC : +z direction
- But OpenGL's projection functions change the hand-ness Thus view, world, model spaces use right-handed coordinate system
  - Viewing direction in view space : -z direction



#### **Canonical View Volume**

- OpenGL only draws objects **inside** the canonical view volume
  - To draw objects only in the camera's view



Not to draw objects too near or too far from the camera

# Do we always have to use the cube of size 2 as a view volume?

- No. You can set any size visible volume and draw objects inside it.
  - Even you can use "frustums" as well as cuboids
- Then everything in the visible volume is mapped (projected) into the canonical view volume.
- Then 3D points in the canonical view volume are projected onto its xy plane as 2D points.
- $\rightarrow$  **Projection transformation**

# **Projection in General**

• General definition:

• Transforming points in n-space to m-space (m<n)

# **Projection in Computer Graphics**

• Mapping 3D coordinates to 2D screen coordinates.



- Two stages:
  - Map an arbitrary view volume to a canonical view volume
  - Map 3D points in the canonical view volume onto its xy plane : But we still need z values of points for depth test, so do not consider this second stage
- Two common projection methods
  - Orthographic projection
  - Perspective projection

# **Orthographic(Orthogonal) Projection**

- View volume : Cuboid (직육면체)
- Orthographic projection : Mapping from a cuboid view volume to a canonical view volume
  - Combination of scaling & translation
    - $\rightarrow$  "Windowing" transformation



#### Windowing Transformation

Transformation that maps a point (p<sub>x</sub>, p<sub>y</sub>) in a rectangular space from (x<sub>1</sub>, y<sub>1</sub>) to (x<sub>h</sub>, y<sub>h</sub>) to a point (p<sub>x</sub>', p<sub>y</sub>') in a rectangular space from (x<sub>1</sub>', y<sub>1</sub>') to (x<sub>h</sub>', y<sub>h</sub>')



#### **Orthographic Projection Matrix**

• By extending the matrix to 3D and substituting

- 
$$x_h$$
=right,  $x_l$ =left,  $x_h$ '=1,  $x_l$ '=-1  
-  $y_h$ =top,  $y_l$ =bottom,  $y_h$ '=1,  $y_l$ '=-1  
-  $z_h$ =-far,  $z_l$ =-near,  $z_h$ '=1,  $z_l$ '=-1

$$\begin{split} \mathsf{M}_{\mathsf{orth}} &= \begin{bmatrix} \frac{2}{\mathit{right-left}} & 0 & 0 & -\frac{\mathit{right+left}}{\mathit{right-left}} \\ 0 & \frac{2}{\mathit{top-bottom}} & 0 & -\frac{\mathit{top+bottom}}{\mathit{top-bottom}} \\ 0 & 0 & \frac{-2}{\mathit{far-near}} & -\frac{\mathit{far+near}}{\mathit{far-near}} \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{split}$$

# **Examples of Orthographic Projection**



An object always stay the same size, no matter its distance from the viewer.

# **Properties of Orthographic Projection**

- Not realistic looking
- Good for exact measurement



- Most often used in CAD, architectural drawings, etc. where taking exact measurement is important
- Affine transformation
  - parallel lines remain parallel
  - ratios are preserved
  - angles are often not preserved

# glOrtho()

- glOrtho(left, right, bottom, top, zNear, zFar)
- : Creates a orthographic projection matrix and right-multiplies the current transformation matrix by it
- Sign of zNear, zFar:
  - positive value: the plane is in front of the camera
  - negative value: the plane is behind the camera.
- $C \leftarrow CM_{orth}$



# [Practice] glOrtho

```
import glfw
from OpenGL.GL import *
from OpenGL.GLU import *
import numpy as np
qCamAnq = 0.
qCamHeight = 1.
# draw a cube of side 1, centered at the origin.
def drawUnitCube():
    glBegin(GL QUADS)
    glVertex3f( 0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f( 0.5, 0.5, 0.5)
    glVertex3f( 0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f( 0.5,-0.5,-0.5)
    glVertex3f( 0.5, 0.5, 0.5)
    glVertex3f(-0.5, 0.5, 0.5)
    glVertex3f(-0.5,-0.5, 0.5)
    glVertex3f( 0.5,-0.5, 0.5)
    glVertex3f( 0.5,-0.5,-0.5)
    glVertex3f(-0.5,-0.5,-0.5)
    glVertex3f(-0.5, 0.5,-0.5)
    glVertex3f( 0.5, 0.5,-0.5)
```

```
glVertex3f(-0.5, 0.5, 0.5)
glVertex3f(-0.5, 0.5,-0.5)
glVertex3f(-0.5,-0.5,-0.5)
glVertex3f(-0.5,-0.5, 0.5)
```

```
glVertex3f( 0.5, 0.5,-0.5)
glVertex3f( 0.5, 0.5, 0.5)
glVertex3f( 0.5,-0.5, 0.5)
glVertex3f( 0.5,-0.5,-0.5)
glEnd()
```

```
def drawCubeArray():
    for i in range(5):
        for j in range(5):
            for k in range(5):
                glPushMatrix()
                glTranslatef(i,j,-k-1)
                glScalef(.5,.5,.5)
                drawUnitCube()
                glPopMatrix()
```

```
def drawFrame():
    glBegin(GL_LINES)
    glColor3ub(255, 0, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([1.,0.,0.]))
    glColor3ub(0, 255, 0)
    glVertex3fv(np.array([0.,0.,0.]))
    glVertex3fv(np.array([0.,1.,0.]))
    glColor3ub(0, 0, 255)
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,0]))
    glVertex3fv(np.array([0.,0.,1.]))
    glEnd()
```

```
def key callback (window, key, scancode, action,
                                                    mods):
                                                        global gCamAng, gCamHeight
                                                        if action==glfw.PRESS or
                                                    action==glfw.REPEAT:
def render():
    global gCamAng, gCamHeight
                                                            if key==glfw.KEY 1:
                                                                gCamAng += np.radians(-10)
                                                            elif key==glfw.KEY 3:
glClear(GL COLOR BUFFER BIT|GL DEPTH BUFFER BIT)
                                                                gCamAng += np.radians(10)
    glEnable (GL DEPTH TEST)
                                                            elif key==glfw.KEY 2:
                                                                gCamHeight += .1
    # draw polygons only with boundary edges
    glPolygonMode ( GL FRONT AND BACK, GL LINE )
                                                            elif key==glfw.KEY W:
                                                                gCamHeight += -.1
    glLoadIdentity()
                                                    def main():
                                                        if not glfw.init():
    # test other parameter values
    # near plane: 10 units behind the camera
                                                            return
    # far plane: 10 units in front of
                                                        window =
                                                    glfw.create window(640,640, 'glOrtho()',
 the camera
                                                    None, None)
    glOrtho(-5,5, -5,5, -10,10)
                                                        if not window:
                                                            glfw.terminate()
gluLookAt(1*np.sin(gCamAng),gCamHeight,1*np.cos(
qCamAnq), 0,0,0, 0,1,0)
                                                            return
                                                        glfw.make context current (window)
                                                        glfw.set key callback(window, key callback)
    drawFrame()
    glColor3ub(255, 255, 255)
                                                        while not glfw.window should close (window):
    drawUnitCube()
                                                            glfw.poll events()
                                                            render()
                                                            glfw.swap buffers (window)
    # test
    # drawCubeArray()
                                                        glfw.terminate()
                                                    if name == " main ":
                                                        main()
```

#### Quiz #2

- Go to <u>https://www.slido.com/</u>
- Join #cg-hyu
- Click "Polls"
- Submit your answer in the following format:
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#### **Perspective Effects**

• Distant objects become small.

**Vanishing point**: The point or points to which the extensions of parallel lines appear to converge in a perspective drawing





# **Perspective Projection**

- View volume : Frustum (절두체)
- $\rightarrow$  "Viewing frustum"



• Perspective projection : Mapping from a viewing frustum to a canonical view volume



#### Why this mapping make "perspective"?

**Original 3D scene** 

#### Red: viewing frustum, Blue: objects



#### **An Example of Perspective Projection**

After perspective projection



#### **An Example of Perspective Projection**

#### The camera view



#### Let's first consider 3D View Frustum→2D Projection Plane

• Consider the projection of a 3D point on the camera plane



#### **Perspective projection**



similar triangles:

$$\frac{y'}{d} = \frac{y}{-z}$$
$$y' = -\frac{dy}{z}$$

#### Homogeneous coordinates revisited

- Perspective requires division
  - that is **not** part of affine transformations
  - in affine, parallel lines stay parallel
    - therefore not vanishing point
    - therefore no rays converging on viewpoint
- "True" purpose of homogeneous coords: projection

#### Homogeneous coordinates revisited

• Introduced w = 1 coordinate as a placeholder

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} \to \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- used as a convenience for unifying translation with linear
- Can also allow arbitrary w

$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \sim \begin{bmatrix} wx \\ wy \\ wz \\ w \end{bmatrix}$$

#### **Perspective projection**



to implement perspective, just move z to w:

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} -dx/z \\ -dy/z \\ 1 \end{bmatrix} \sim \begin{bmatrix} dx \\ dy \\ -z \end{bmatrix} = \begin{bmatrix} d & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{vmatrix} x \\ y \\ z \\ 1 \end{vmatrix}$$

Cornell CS4620 Fall 2008 • Lecture 8

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# **Perspective Projection Matrix**

- This  $3D \rightarrow 2D$  projection example gives the basic idea of perspective projection.
- What we really have to do is  $3D \rightarrow 3D$ , View Frustum $\rightarrow$ Canonical View Volume.
- For details for this process, see 6-reference-projection.pdf

• 
$$\mathbf{M}_{\text{pers}} = \begin{pmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{-(f+n)}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

# glFrustum()

- glFrustum(left, right, bottom, top, near, far)
  - near, far: The distances to the near and far depth clipping planes. **Both** distances must be positive.
- : Creates a perspective projection matrix and rightmultiplies the current transformation matrix by it
- $C \leftarrow CM_{pers}$



# gluPerspective()

- gluPerspective(fovy, aspect, zNear, zFar)
  - fovy: The field of view angle, in degrees, in the y-direction.
  - aspect: The aspect ratio that determines the field of view in the xdirection. The aspect ratio is the ratio of x (width) to y (height).
- : Creates a perspective projection matrix and rightmultiplies the current transformation matrix by it



[Practice] glFrustum(), gluPerspecti ve()

```
def render():
    global gCamAng, gCamHeight
    glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
    glEnable(GL_DEPTH_TEST)
    glPolygonMode( GL_FRONT_AND_BACK, GL_LINE )
```

```
glLoadIdentity()
```

```
# test other parameter values
glFrustum(-1,1, -1,1, .1,10)
# glFrustum(-1,1, -1,1, 1,10)
```

```
# test other parameter values
# gluPerspective(45, 1, 1,10)
```

```
# test with this line
gluLookAt(5*np.sin(gCamAng),gCamHeight,5*np.cos(gCam
Ang), 0,0,0, 0,1,0)
```

```
drawFrame()
glColor3ub(255, 255, 255)
```

```
drawUnitCube()
```

```
# test
# drawCubeArray()
```

#### Quiz #3

- Go to <u>https://www.slido.com/</u>
- Join #cg-hyu
- Click "Polls"
- Submit your answer in the following format:
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  - e.g. 2017123456: 4)
- Note that you must submit all quiz answers in the above format to be checked for "attendance".

#### **Viewport Transformation**



### **Recall that...**

- 1. Placing objects
- $\rightarrow$  Modeling transformation
- 2. Placing the "camera"
- $\rightarrow$  Viewing transformation
- 3. Selecting a "lens"
- $\rightarrow$  **Projection transformation**
- 4. Displaying on a "cinema screen"
- $\rightarrow$  Viewport transformation

# **Viewport Transformation**



- Viewport: a rectangular viewing region of screen
- So, viewport transformation is also a kind of windowing transformation.

#### **Viewport Transformation Matrix**

- In the windowing transformation matrix,
- By substituting x<sub>h</sub>, x<sub>l</sub>, x<sub>h</sub>', ... with corresponding variables in viewport transformation,

 $x_i$ 

# glViewport()

- glViewport(xmin, ymin, width, height)
  - xmin, ymin, width, height: specified in pixels
- : Sets the viewport
  - This function does NOT explicitly multiply a viewport matrix with the current matrix.
  - Viewport transformation is internally done in OpenGL, so you can apply transformation matrices starting from a canonical view volume, not a screen space.
- Default viewport setting for (xmin, ymin, width, height) is (0, 0, window width, window height).
  - If you do not call glViewport(), OpenGL uses this default viewport setting.

$y_i$	width	t
	(x <sub>min</sub> , y <sub>min</sub> )	
	$\overline{x_i}$	

#### [Practice] glViewport()

```
def main():
    # ...
    glfw.make_context_current(window)
    glViewport(100,100,200,200)
    # ...
```

#### Next Time

- Lab in this week:
  - Lab assignment 6
- Next lecture:
  - 7 Hierarchical Modeling, Mesh
- Class Assignment #1

  Due: 23:59, May 3, 2019
- Midterm Exam Notice
- Acknowledgement: Some materials come from the lecture slides of
  - Prof. Jinxiang Chai, Texas A&M Univ., <u>http://faculty.cs.tamu.edu/jchai/csce441\_2016spring/lectures.html</u>
  - Prof. Taesoo Kwon, Hanyang Univ., <u>http://calab.hanyang.ac.kr/cgi-bin/cg.cgi</u>
  - Prof. Steve Marschner, Cornell Univ., <u>http://www.cs.cornell.edu/courses/cs4620/2014fa/index.shtml</u>