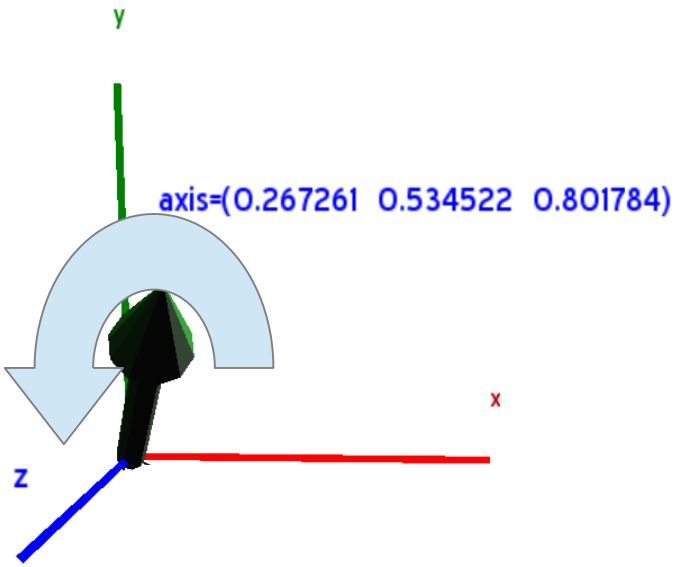
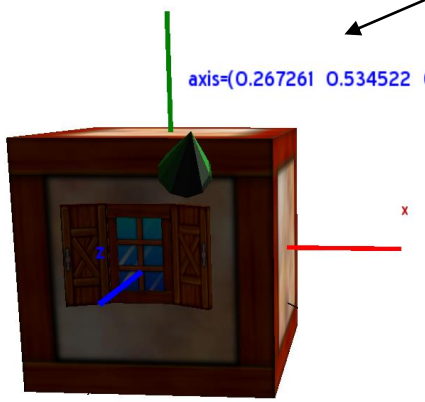
Let's compute the rotation matrix R

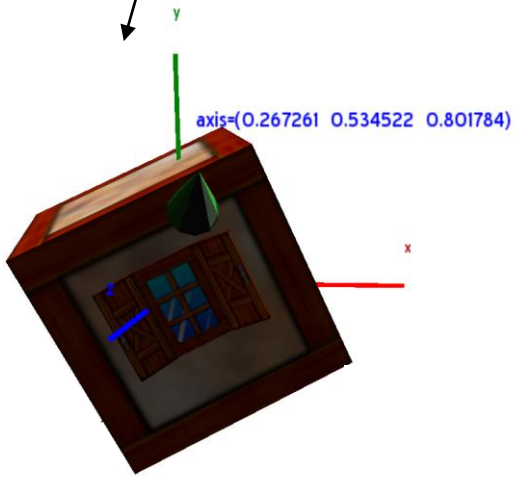
Rotation about $axis = (1,2,3)$ by $\theta = 30$ degrees



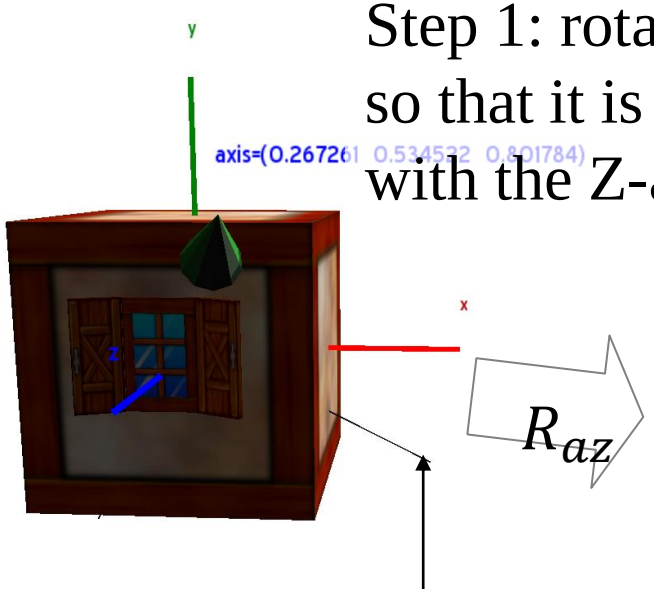
Before rotation



After rotation



Step 1: rotate the axis so that it is aligned with the Z-axis

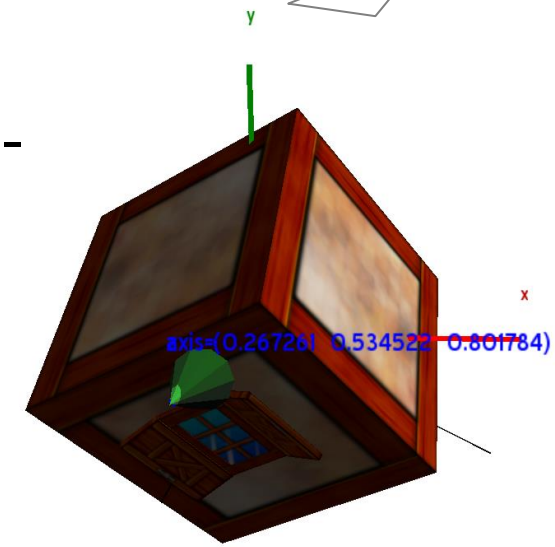


R_{az}

rotation axis of R_{az}

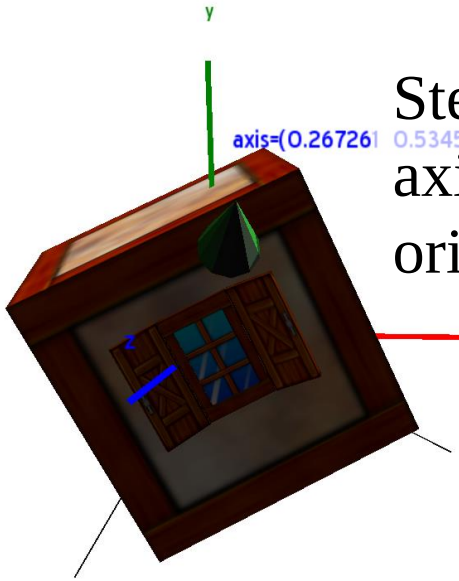
Step 2: rotate about the Z-axis by $\theta = 30$

R_z



Step 3: rotate the Z-axis back to the original axis

R_{az}^{-1}



How to compute R_{az} (Axis a to axis z)

1. Let the normalize axis

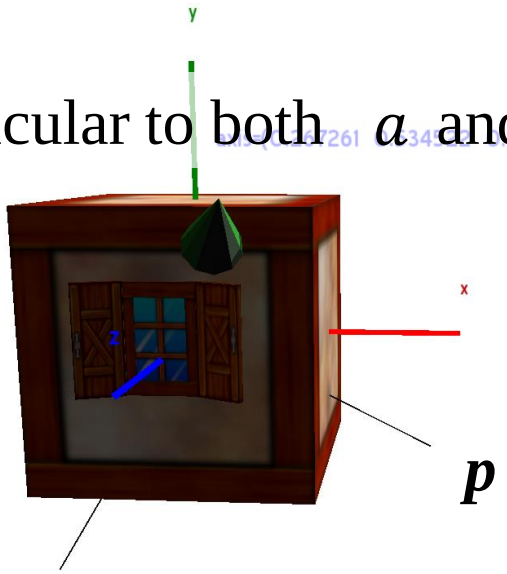
$$a = \frac{axis}{\|axis\|} \approx (0.27, 0.53, 0.80)$$

$$\|v\| = \sqrt{v \cdot v} = x^2 + y^2 + z^2$$

where $v = (x, y, z)$

2. Calculate vector p that is perpendicular to both a and Z-axis

$$p = \frac{a \times (0,0,1)}{\|a \times (0,0,1)\|}$$



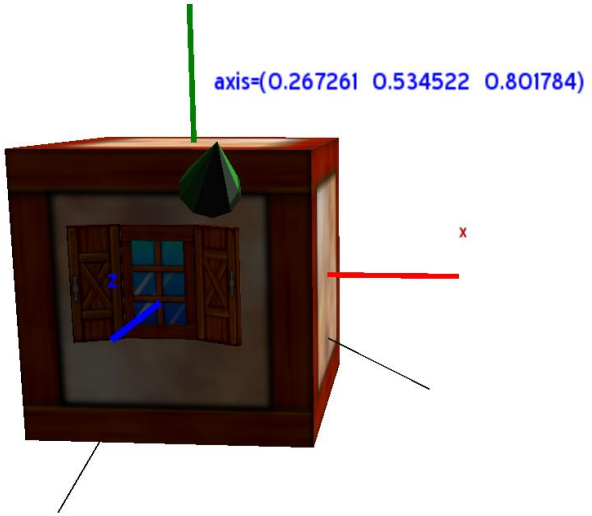
How to compute R_{az}

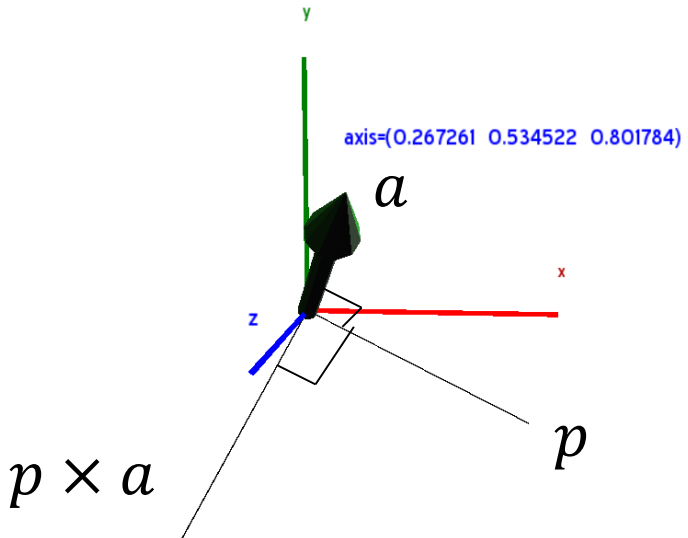
3. after rotation R_{az}

$R_{az}a$ becomes $(0,0,1)$

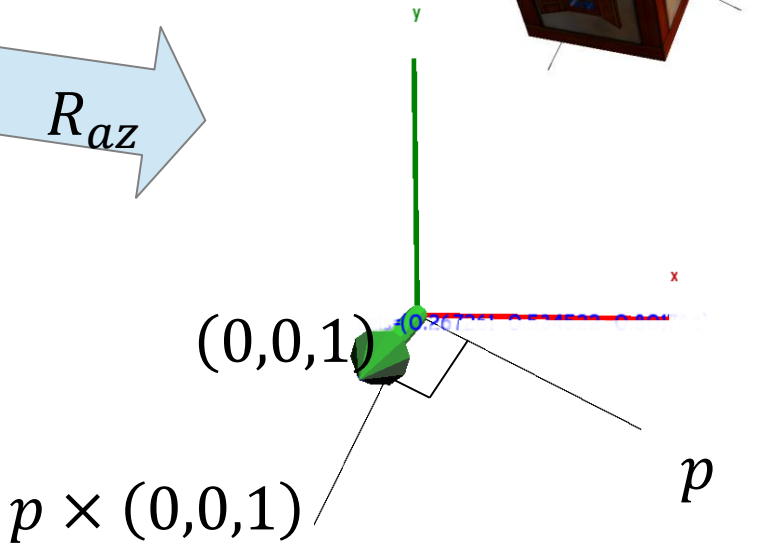
$R_{az}p$ becomes p

$R_{az}(p \times a)$ becomes $p \times (0,0,1)$





R_{az}



How to compute R_{az}

3. Then after the rotation R_{az}

$$R_{az}a \quad \text{becomes} \quad (0,0,1)$$

$$R_{az}p \quad \text{becomes} \quad p$$

$$R_{az}(p \times a) \quad \text{becomes} \quad p \times (0,0,1)$$

Therefore,

$$R_{az}([a][p][p \times a]) = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \quad [p] \quad [p \times (0,0,1)]$$

Finally,

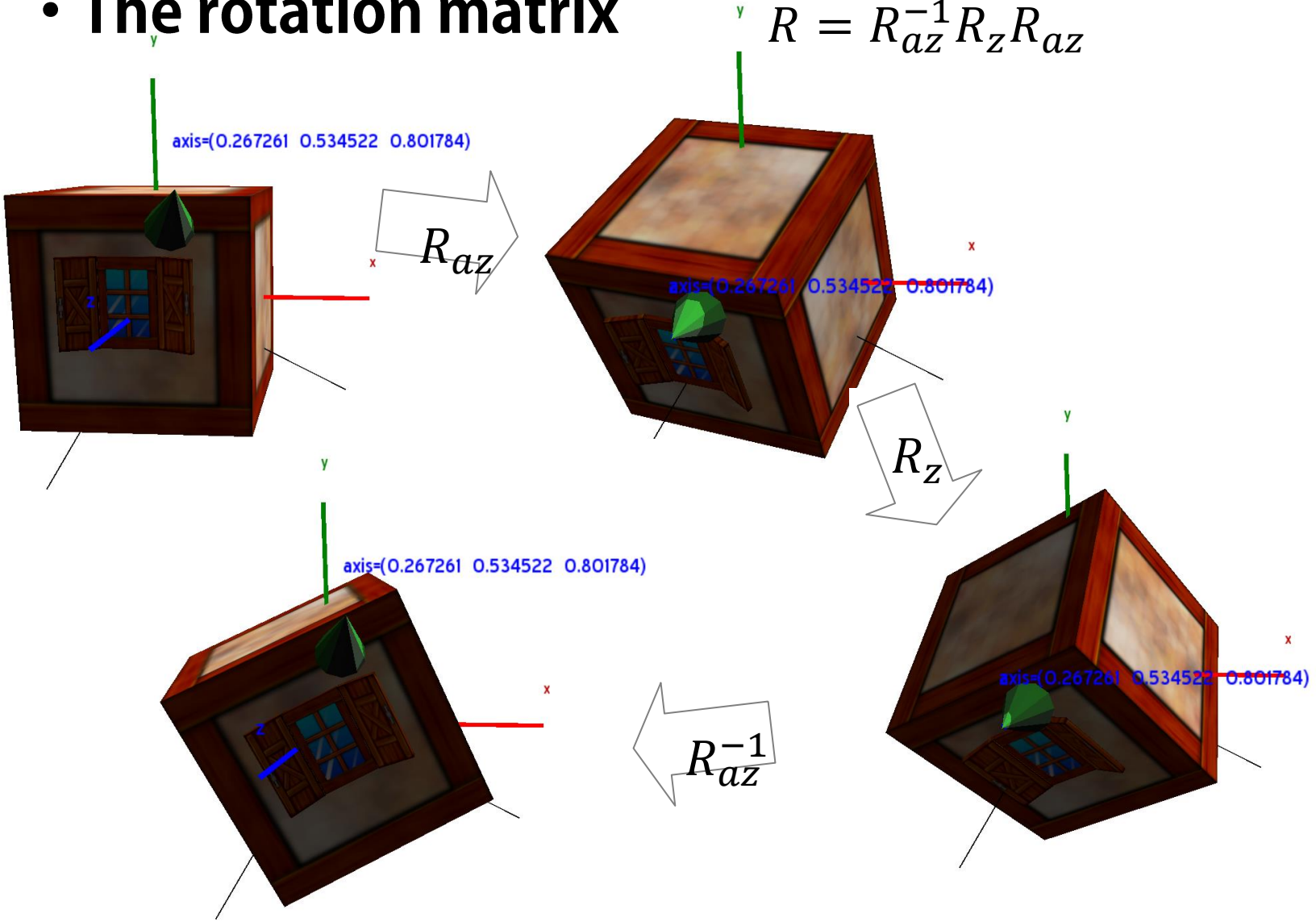
$$R_{az} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \quad [p] \quad [p \times (0,0,1)] \Big) ([a][p][p \times a])^{-1}$$

Matlab codes:

```
> z=[0;0;1]
> Raz=[z p cross(p,z)] *inv([a p cross(p,a)])
```

Finally,

- **The rotation matrix** $R = R_{az}^{-1} R_z R_{az}$



Acknowledgement

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